

region has to be developed. This is expected to lead to somewhat different values for the additional intensity component  $I_z$  but will not change the general effect of this component on the SAXS curves.

**Acknowledgment.** I am indebted to Dr. A. R. Kholov for useful discussions.

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# Light Scattering Characterization of an Alternating Copolymer of Ethylene and Tetrafluoroethylene. 1. Static and Dynamic Properties

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**ABSTRACT:** Laser light scattering, including the angular dependence of the absolute integrated scattered intensity and its spectral distribution, has been used successfully to characterize, for the first time, an alternating copolymer of ethylene and tetrafluoroethylene,  $-(CH_2CH_2CF_2CF_2)_x-$ , in diisobutyl adipate at 240 °C. In order to carry out experiments at high temperatures, we developed a new filtration apparatus and a new light scattering spectrometer capable of refractive index increment measurements. The results show that over the molecular weight range  $5 \times 10^5$  to  $1.2 \times 10^6$ , our copolymer samples obey the scaling relations  $\langle R_g^2 \rangle_z^{1/2} = 1.68 \times 10^{-1} M_w^{0.60}$  and  $D_0^\circ = 3.35 \times 10^{-4} M_w^{-0.60}$ , with  $\langle R_g^2 \rangle_z^{1/2}$ ,  $M_w$ , and  $D_0^\circ$  being the z-average root-mean-square radius of gyration (Å), the weight-average molecular weight, and the translational diffusion coefficient at infinite dilution (cm<sup>2</sup>/s), respectively. Furthermore, the variance ( $\mu_2/\bar{I}^2$ ) of the photoelectron count time correlation function shows a small value ( $\sim 0.1$ ), suggesting surprisingly narrow molecular weight distributions for our copolymer samples.

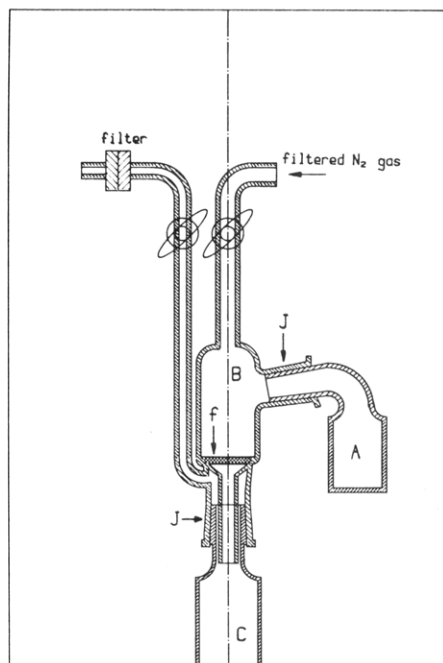
## I. Introduction

Laser light scattering (LLS) has been used to characterize a variety of polymers, including poly(1,4-phenylene terephthalamide) (PPTA)<sup>1-5</sup> and polyethylenes (PE).<sup>6,7</sup> The advantages of LLS are numerous. It is noninvasive. It has a wide dynamic range covering sizes from tens of angstroms to microns. The technique also permits determination of polydispersity in terms of molecular weight distributions, especially for unimodal functions of arbitrary shapes, without an a priori assumption on the form of the distribution function. In particular, LLS has been effective in characterizing polymer solutions at high temperatures,<sup>6,7</sup> e.g., at more than 200 °C for poly(dichlorophosphazene) in hexachlorotriphosphazene<sup>8</sup>, and polyelectrolytes (PPTA) in concentrated sulfuric acid, with and without added salt.<sup>1-5</sup> Thus, a natural extension and challenge in the application of LLS to polymer solution characterization is to examine static and dynamic properties of fluorocarbon polymers that defy characterization, simply because they are essentially insoluble in any ordinary solvents. Although our ultimate aim is to characterize poly(tetrafluoroethylene),  $-(CF_2CF_2)_x-$ , commercially known as Teflon (a registered trademark of Du Pont), we have to approach the characterization of poly(tetrafluoroethylene) (PTFE) slightly differently in view of the structural complexities associated with the solvent and plan to report our findings on PTFE later. In this (1) and a subsequent article (2), we report details of the characterization of a Teflon co-

polymer, an alternating copolymer of ethylene and tetrafluoroethylene (PETFE),  $-(CF_2CF_2CH_2CH_2)_y-$ . An outline of our procedures has already appeared in a preliminary publication.<sup>9</sup> Our report on the PETFE characterization can be divided into two parts. In this article (1), we shall be concerned with experiments on static and dynamic properties of PETFE in diisobutyl adipate at 240 °C, including a description of our new high-temperature light scattering spectrometer, adaptation for use as a high-temperature differential refractometer, and the development of a new high-temperature filtration apparatus for polymer solution clarification. In the subsequent article (2), we shall consider the determination of the molecular weight distribution (MWD) of PETFE from precise time correlation function measurements using experimentally determined scaling relations between the translational diffusion coefficient and the molecular weight and three different algorithms for the Laplace inversion. We report the details of our analysis in a separate article (2) because MWD can be determined only by means of LLS. At the present time, there is no other known technique that can provide an absolute determination of MWD of PETFE.

## II. Experimental Methods

**1. Materials.** Diisobutyl adipate was obtained from Hatco Industries and was purified by passage through a column of activated silica gel to remove acidic and basic impurities. The resulting material was 99.5% pure by vapor phase chromatography. The polymers (courtesy of W. Buck, Polymer Products



**Figure 1.** High-temperature dissolution/filtration apparatus. The entire apparatus can be placed in a high-temperature oven controlled at  $250 \pm 2^\circ\text{C}$ . (A) Solution vessel, where we can introduce known weights of the dried polymer (PETFE) and the solvent (diisobutyl adipate) as well as a small glass-enclosed magnetic stirrer. (B) Filter, connected with A and C by means of clear seal glass joints (J) (14/20, Wheaton Scientific). f is a fine-grade sintered glass filter. (C) Cylindrical light scattering cell of 27-mm o.d. with a clear seal glass joint.

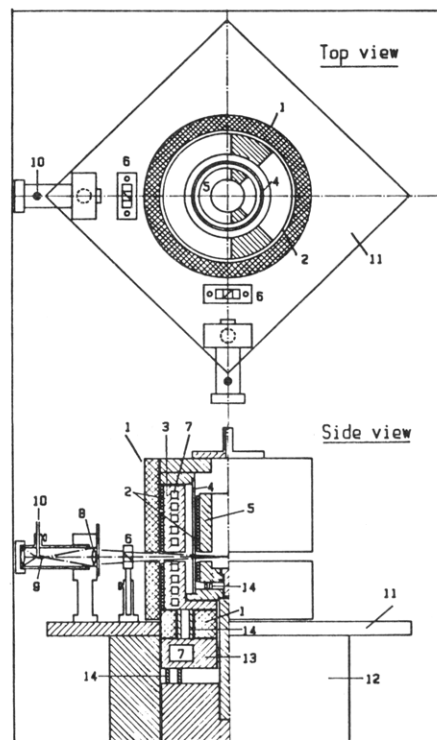
Department, Du Pont Experimental Station, Wilmington, DE) were commercial samples of Tefzel PETFE, manufactured by E. I. du Pont de Nemours and Co., and were used as received.

**2. Preparation of Solutions.** Solutions at different concentrations were prepared individually by dissolving known weights of the dried PETFE in diisobutyl adipate at  $250 \pm 2^\circ\text{C}$ .

A special dissolution/filtration apparatus was designed for this purpose. Such an apparatus constitutes a key element toward the success of our experiments. Furthermore, it should be useful for all high-temperature polymer solution clarifications. Therefore, we describe the apparatus, as shown in Figure 1, in some detail.

Known weights of PETFE and filtered diisobutyl adipate, as well as a small glass-enclosed magnetic stirrer, were placed in A at room temperature. The solution vessel (A) was connected to the precleaned filter (B). After degassing and introduction of nitrogen, both stopcocks were closed. PETFE was dissolved in diisobutyl adipate at  $250^\circ\text{C}$  under constant stirring. It took about 1 h to dissolve the polymer completely. In order to ensure complete dissolution and homogeneity, we usually stirred the polymer solution for another hour before filtration. As the polymer solution in A was open to B, which was "open" to C through a fine-grade sintered glass filter, the volumes of B and C were kept small in order to reduce the volume available to the solvent vapor phase. When the polymer solution in A was ready for filtration, the solution vessel was turned  $180^\circ$  by means of the clear seal glass joint (J) between A and B. Then the polymer solution could be transferred to B without exposure to air at  $250^\circ\text{C}$ . We used a gentle 10-psi nitrogen pressure to force the polymer solution directly into the precleaned dust-free cylindrical light scattering cell (C). This simple dissolution/filtration apparatus permits polymer solution preparation and clarification at high temperatures under an inert atmosphere without exposure to the external environment. Dust-free polymer solutions could be prepared with a very high rate of success with this apparatus. Furthermore, as the PETFE alternating copolymer has so few known solvents, we cleaned the all-glass dissolution/filtration apparatus by pyrolysis ( $\sim 500^\circ\text{C}$ ). As a consequence, the same apparatus could be used repeatedly without degradation of performance.

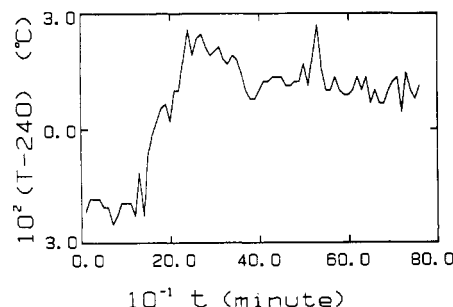
**3. Methods of Measurement.** A new high-temperature light scattering spectrometer was constructed for the PETFE char-



**Figure 2.** Schematic top and side views of the high-temperature thermostat and detection system of the light scattering spectrometer: (1) silicon rubber insulation; (2) heating wires for the brass thermostats; (3) outer brass thermostat with fluid circulation facilities; (4) vacuum glass jacket for thermal isolation (the glass jacket is made of precision polished glass of 2.25-in. o.d. with Kovar seals at both ends and machine-centered to coincide with the center of rotation of the turntable (12) to 0.001 in.); (5) inner brass thermostat, which has a separate temperature controller and thermometer and can accommodate light scattering cells up to 27-mm o.d.; (6) Glan-Thompson polarizers; (7) fluid circulation paths; (8) lens; (9) field aperture; (10) optical fiber bundle; (11) rotating plate for multiple detectors; (12) RT-200 Klinger rotary table with  $0.01^\circ$  step size; (13) cooling plate to isolate the outer thermostat from the rotary table; (14) stainless steel standoffs for thermal isolation.

acterization. Figure 2 shows the schematic top and side views of the essential features of the spectrometer, including the high-temperature thermostat and the detection optics.

The essential features of the thermostat are as follows. We used a thermally controllable plate (13) as a heat sink which isolates the rotary table (12) from the outer thermostat (3) by means of two sets of stainless steel standoffs (14). The outer brass thermostat (3) was isolated from the room with 0.5-in.-thick porous silicone rubber. This arrangement created an oven that could be maintained easily in the  $200\text{--}230^\circ\text{C}$  range with temperature fluctuations of less than  $0.2^\circ\text{C}$ . A glass (vacuum) jacket of 2.25-in. o.d. was used to isolate the inner thermostat from the oven. The main function for the vacuum jacket was to reduce the temperature gradient in the light scattering cell. The inner thermostat had a separate temperature controller and a miniature platinum resistance thermometer that could be connected through the vacuum jacket by means of ceramic feed throughs. Figure 3 shows a typical tracing of the temperatures monitored by the thermometer located on the inner thermostat. Short-term (20 min) control of  $\pm 0.005^\circ\text{C}$  and intermediate-term (60 min) control of  $\pm 0.01^\circ\text{C}$  could be achieved at  $240^\circ\text{C}$ , even in the absence of a vacuum. In a typical experiment, temperature could be controlled to  $\pm 0.03^\circ\text{C}$  during the entire experiment period, lasting around 10 h. For polymer solutions at high temperatures, it was important to test whether any appreciable degradation had taken place. All preparations and measurements were usually completed within a 12-h period and could be reproduced. The polymer concentration was checked independently by weighing the solution and, after evaporation, the polymer. The polymer solution began to have a yellowish tint after 36 h, and measurements could be



**Figure 3.** Typical temperature fluctuations of the inner thermostat at 240 °C. The large 20-min jump was due to a slight temperature readjustment. Short-term (20 min) temperature fluctuations were  $\sim \pm 0.005$  °C. Intermediate-term (60 min) temperature fluctuations were  $\lesssim \pm 0.01$  °C. Long-term (10 h) temperature fluctuations were  $\lesssim \pm 0.03$  °C. The temperature gradient along the vertical axis (perpendicular to the scattering plane) was estimated to be  $\lesssim 0.02$  °C/cm in the absence of a vacuum.

reproduced within the first 36 h. One set of measurements was extended to  $\sim 100$  h. We then observed a  $\sim 5\%$  decrease in the characteristic decay times. However, as the light scattering cells were sealed only by the clear seal glass joint, we could not exclude a small amount of solvent evaporation.

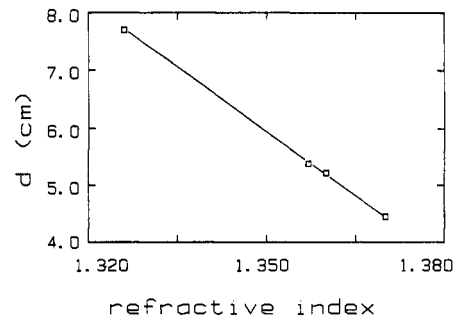
The detection system consists of a 1 ft  $\times$  1 ft rotating platform (11) and various optical and mechanical components. Figure 2 shows the dual detection optics located 90° apart. Each detection "arm" has a lens (8) that transfers the scattering volume to the variable (e.g.,  $\sim 0.7$ -mm diameter) field aperture (9) with a 2.5:1 ratio. The angular aperture is located in front of the lens (8), yielding a  $\delta\theta$  of  $\sim 0.1^\circ$ . The scattered light coming from well-defined scattering volume and angular aperture is transferred to the photomultiplier tube (EMI 9863) via an optical fiber bundle. It is important to have the appropriate optics *before* the optical fiber bundle, which acts only as a light pipe for the scattered light intensity. In this manner, the light scattering spectrometer could be reduced in size to a 1 ft  $\times$  1 ft platform, and simultaneous multiple-angle detection becomes feasible. With the platform, we can vary the angle between the two detection "arms" from about  $10^\circ$  to  $160^\circ$ . Simultaneous multiple-angle detection has the additional advantage of permitting time-dependent LLS studies of polymer solutions and gels. In our case, we could roughly shorten the measurement time by half using the dual-angle detection system. We used a Spectra-Physics Model 2020-03 argon ion laser operating nominally at  $\sim 150$  mW and  $\lambda_0 = 488.0$  nm.

Intensity measurements were accumulated automatically every  $10^\circ$  between the scattering angles  $\theta$  of  $30^\circ$  and  $120^\circ$  for 10-s periods. No gating arrangement to exclude the effect of dust contributions was needed because the polymer solutions show little fluctuations in integrated scattered intensity which could be attributed to dust particles passing through the scattering volume.

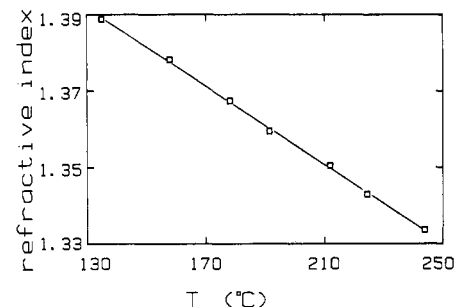
Correlation function measurements were made with a 128-channel  $4 \times n$  correlator (Brookhaven Instruments, Model 2030). In the measured time correlation functions, the computed and measured base lines usually agreed to within 0.1%. The light scattering spectrometer was calibrated with benzene and NBS-705 polystyrene standard in cyclohexane.

### III. Results and Discussion

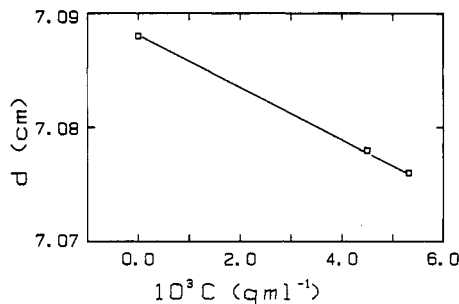
**1. Refractive Index and Refractive Index Increment Measurements.** An absolute determination of the polymer molecular weight requires information on the refractive index increment ( $dn/dc$ ) as well as the excess Rayleigh ratio ( $R_{90}$ ). A cylindrical light scattering cell was deformed to permit the exit laser beam to be refracted by the solution/air interface. The refraction could be measured and calibrated by using solvents of known refractive indices at room temperatures, as shown in Figure 4. Figure 5 shows a plot of refractive index of the solvent, diisobutyl adipate, as a function of temperature. We obtained  $n = 1.389 - 5.11 \times 10^{-4}(T^* - 135^\circ\text{C})$ , with  $T^*$  expressed in °C. The refractive index of diisobutyl adipate



**Figure 4.** Calibration of a refractive index cell with different organic solvents at 25 °C and  $\lambda_0 = 488$  nm.  $d$  denotes the laser beam displacement as measured by a micrometer.  $dd/dn = -7.385 \times 10$  cm with a resolution of  $\pm 0.001$  mm.



**Figure 5.** Refractive index of diisobutyl adipate as a function of temperature at  $\lambda_0 = 488$  nm.  $dn/dT^* = -5.11 \times 10^{-4} \text{ } ^\circ\text{C}^{-1}$ .  $n = 1.389 - 5.11 \times 10^{-4}(T^* - 135^\circ\text{C})$ , with  $T^*$  expressed in °C. The refractive index of diisobutyl adipate at 240 °C was estimated to be 1.334 at  $\lambda_0 = 488$  nm.



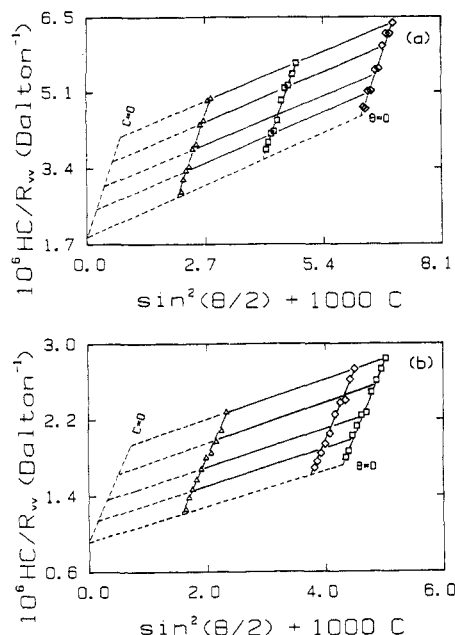
**Figure 6.** Plot of displacement  $d$  as a function of PETFE polymer concentration in diisobutyl adipate at 240 °C.  $dd/dc = -2.25$  (cm mL)/g, corresponding to  $dn/dc = 0.031$  mL/g at  $\lambda_0 = 488$  nm.

at 240 °C was estimated to be 1.334. Figure 6 shows a plot of displacement  $d$  as a function of PETFE polymer concentration in diisobutyl adipate at 240 °C with  $(\partial d/\partial C)_T = -2.25$  (cm mL)/g. From our calibration, as shown in Figure 4,  $(\partial d/\partial n)_T = -7.385 \times 10$  cm. Thus, we obtained the refractive index increment for PETFE in diisobutyl adipate:  $(\partial d/\partial C)_T/(\partial d/\partial n)_T = 2.25/73.85 \approx 0.031$  mL/g at 240 °C using  $\lambda_0 = 488$  nm. Although the calibration was performed at room temperature, the instrument showed negligible temperature effect over a 100 °C temperature change.

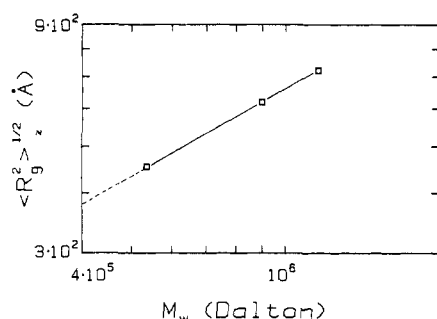
**2. Light Scattering Intensity Measurements.** The excess absolute integrated intensity of light scattered at a given angle from a dilute polymer solution has the form

$$\frac{HC}{R_{90}(K)} \approx \frac{1}{M_w} \left( 1 + \frac{K^2 \langle R_g^2 \rangle_z}{3} \right) + 2A_2C \quad (1)$$

where  $H = (4\pi^2 n^2 / N_A \lambda_0^4) (\partial n / \partial C)_T^2$ , with  $\lambda$  ( $\equiv \lambda_0 / n$ ),  $A_2$ ,  $\langle R_g^2 \rangle_z$ ,  $M_w$ , and  $K [ \equiv (4\pi / \lambda) \sin(\theta/2) ]$  being, respectively, the wavelength of light in the scattering medium, the second virial coefficient, the  $z$ -average mean-square radius



**Figure 7.** Zimm plots of PETFE in diisobutyl adipate at 240 °C using  $\lambda_0 = 488$  nm. (a)  $M_w = 5.4 \times 10^6$ ,  $A_2 = 1.97 \times 10^{-4} \text{ g}^{-1} \text{ mol}^{-1} \text{ mL}^2$ ,  $\langle R_g^2 \rangle^{1/2} = 454 \text{ Å}$ : ( $\Delta$ )  $C = 2.09 \times 10^{-3} \text{ g/mL}$ ; ( $\square$ )  $C = 4.03 \times 10^{-3} \text{ g/mL}$ ; ( $\diamond$ )  $C = 6.25 \times 10^{-3} \text{ g/mL}$ . (b)  $M_w = 1.16 \times 10^6$ ,  $A_2 = 1.02 \times 10^{-4} \text{ g}^{-1} \text{ mol}^{-1} \text{ mL}^2$ ,  $\langle R_g^2 \rangle^{1/2} = 721 \text{ Å}$ : ( $\Delta$ )  $C = 1.57 \times 10^{-3} \text{ g/mL}$ ; ( $\diamond$ )  $C = 3.75 \times 10^{-3} \text{ g/mL}$ ; ( $\square$ )  $C = 4.28 \times 10^{-3} \text{ g/mL}$ .



**Figure 8.** log-log plot of  $\langle R_g^2 \rangle_z^{1/2}$  vs.  $M_w$  for PETFE in diisobutyl adipate at 240 °C. Solid line denotes  $\langle R_g^2 \rangle_z^{1/2} = 0.168 \times M_w^{0.60}$ , with  $R_g$  and  $M_w$  expressed in Å and daltons, respectively.

of gyration, the weight-average molecular weight, and the magnitude of the momentum transfer vector. The subscripts vv denote vertically polarized incident and scattered light. From a Zimm plot, as shown in Figure 7, we can determine the weight-average molecular weight, the second virial coefficient, and the z-average root-mean-square radius of gyration:

$$M_w: \lim_{\substack{C \rightarrow 0 \\ K \rightarrow 0}} \frac{HC}{R_{vv}} = \frac{1}{M_w} \quad (2)$$

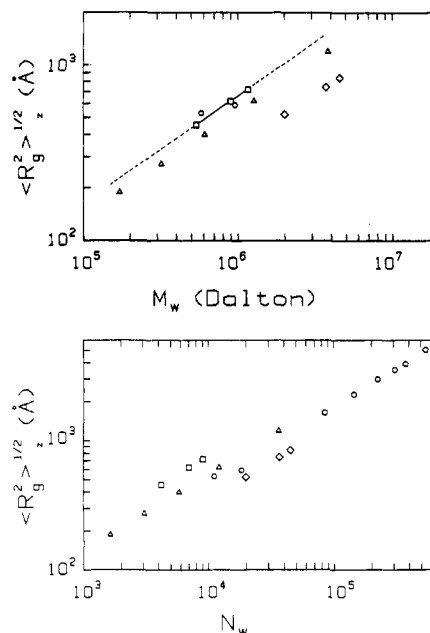
$$\langle R_g^2 \rangle_z^{1/2}: \lim_{C \rightarrow 0} \frac{HC}{R_{vv}} = \frac{1}{M_w} \left( 1 + \frac{K^2 \langle R_g^2 \rangle_z}{3} \right) \quad (3)$$

$$A_2: \lim_{\theta \rightarrow 0} \frac{HC}{R_{vv}} = \frac{1}{M_w} + 2A_2C \quad (4)$$

In a log-log plot of  $\langle R_g^2 \rangle_z^{1/2}$  vs.  $M_w$ , as shown in Figure 8, we obtained the scaling relation

$$\langle R_g^2 \rangle_z^{1/2} = 1.68 \times 10^{-1} M_w^{0.60} \quad (5)$$

with  $R_g$  and  $M_w$  expressed in Å and daltons, respectively. Equation 5 suggested that the PETFE polymer molecules



**Figure 9.** Comparison of radius of gyration of PETFE with those of other typical polymer coils: (a)  $R_g$  as a function of  $M_w$ ; (b)  $R_g$  as a function of  $N_w$  ( $\equiv M_w/M_0$ , with  $M_0$  being the segment unit consisting of 4-carbon atom backbones). Same solid line as in Figure 8. ( $\Delta$ ,  $\circ$ ) Polystyrene in benzene (ref 10 and 11, respectively); ( $\diamond$ ) poly(methylene methacrylate) in methyl methacrylate (ref 12); ( $\circ$ ) polyethylene in 1,2,4-trichlorobenzene (ref 7); ( $\square$ ) present work ( $R_g [\text{Å}] = 1.68 \times 10^{-1} M^{0.60}$ , with  $M$  expressed in daltons).

behave like coils, not wormlike chains. An absence of depolarized light scattering (or molecular anisotropy) further strengthened this supposition. Figure 9 shows a comparison of the radius of gyration of PETFE with those of other polymer coils. Its coil size did not exhibit any surprises; i.e., PETFE behaves more like other typical polymer coils in solution.

### 3. Light Scattering Line-Width Measurements.<sup>6</sup>

The measured intensity-intensity time correlation function in the self-beating mode has the form

$$G^{(2)}(K, \tau) = A(1 + b|g^{(1)}(K, \tau)|^2) \quad (6)$$

where  $A$  is the background and  $b$  is a parameter depending on the detection optics. From eq 6, we can retrieve the normalized first-order electric field time correlation function  $g^{(1)}(\tau)$ , which for polydisperse polymer molecules in solution is related to the normalized characteristic line-width distribution function  $G(\Gamma)$  by the Laplace integral equation:

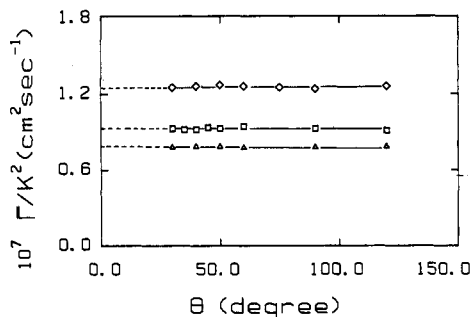
$$g^{(1)}(K, \tau) = \int_0^\infty G(\Gamma) e^{-\Gamma(K)\tau} d\Gamma \quad (7)$$

In the present analysis we shall be concerned only with the method of cumulants, yielding an average line width  $\bar{\Gamma}$  and the variance  $\mu_2/\bar{\Gamma}^2$ , with

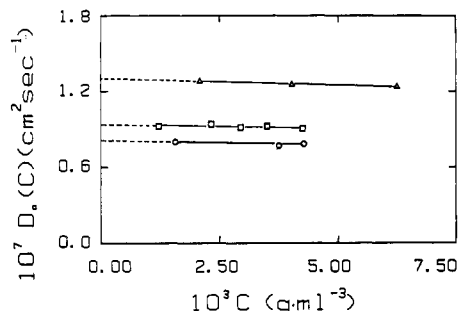
$$\bar{\Gamma} = \int \Gamma G(\Gamma) d\Gamma \quad (8)$$

$$\mu_2 = \int (\Gamma - \bar{\Gamma})^2 G(\Gamma) d\Gamma \quad (9)$$

In the limit of low  $K$  ( $KR_g < 1$ ),  $\bar{\Gamma} = \bar{D}K^2$ , where  $\bar{D}$  is the z-average translational diffusion coefficient. Figure 10 shows typical plots of  $\bar{\Gamma}/K^2$  vs. scattering angle  $\theta$  for PETFE at different molecular weights and concentrations. By extrapolation of  $\bar{\Gamma}/K^2$  to zero scattering angle, we determined the translational diffusion coefficient  $D_0(C)$  [ $\equiv \lim_{K \rightarrow 0} \bar{\Gamma}/K^2$ ] at finite concentrations. From Figure 10,



**Figure 10.** Typical plots of  $\Gamma/K^2$  vs.  $\theta$  for PETFE in diisobutyl adipate at 240 °C: (□)  $M_w = 9.0 \times 10^5$ ,  $C = 3.50 \times 10^{-3}$  g/mL; (◇)  $M_w = 5.4 \times 10^5$ ,  $C = 4.03 \times 10^{-3}$  g/mL; (Δ)  $M_w = 1.16 \times 10^6$ ,  $C = 4.18 \times 10^{-3}$  g/mL.



**Figure 11.** Plots of  $D_0(C)$  as a function of concentration for PETFE in diisobutyl adipate at 240 °C: (□)  $M_w = 9.0 \times 10^5$ ; (○)  $M_w = 1.16 \times 10^6$ ; (Δ)  $M_w = 5.4 \times 10^5$ . As  $k_d \sim 0$ ,  $D_0^\circ \sim D_0$ .

we have also noted that the  $\Gamma = \bar{D}K^2$  relation is obeyed over the scattering angular range of our investigation for the PETFE polymers (up to  $\sim 10^6$  dalton). Thus, in future characterizations of PETFE, this particular step can be ignored without appreciable error so long as  $KR_g < 1$ . In dilute solutions

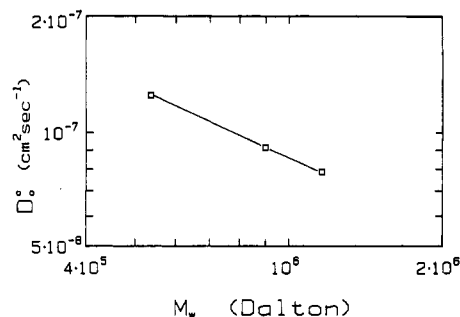
$$D_0(C) = D_0^\circ(1 + k_d C) \quad (10)$$

where  $D_0^\circ$  is the z-average translational diffusion coefficient at infinite dilution.

Figure 11 shows plots of  $D_0(C)$  as a function of concentration for PETFE in diisobutyl adipate over a range of molecular weights at 240 °C. It is interesting to note that for PETFE in diisobutyl adipate at 240 °C,  $k_d \simeq 0$  over the present molecular weight range of  $5 \times 10^5$  to  $1 \times 10^6$ . Thus, by combining these two results, namely,  $\Gamma = \bar{D}K^2$  and  $D_0(C) \simeq D_0^\circ$ , we can easily determine the molecular weight of the PETFE alternating copolymer in diisobutyl adipate at 240 °C by measuring only one characteristic line width at one scattering angle ( $KR_g < 1$ ) and one finite concentration in the dilute solution region, provided that we know the scaling relation  $D_0^\circ = k_d M^{-\alpha_D}$ . Figure 12 shows a log-log plot of  $D_0^\circ$  vs.  $M_w$  for PETFE in diisobutyl adipate at 240 °C. We obtained

$$D_0^\circ = 3.35 \times 10^{-4} M_w^{-0.60} \quad (11)$$

with  $D_0^\circ$  and  $M_w$  expressed in  $\text{cm}^2/\text{s}$  and dalton, respectively. An exponent of 0.6 for  $\alpha_D$  (eq 11) and  $\alpha_R$  (eq 5) appears to suggest that the PETFE molecule is a polymer coil in a good solvent. Yet, we have noted that  $k_d \sim 0$  and  $A_2$  is positive but fairly small, suggesting that the solvent is not very good. A value of 0.60 for  $\alpha_D$  could be expected to be too high since 0.60 is the upper limit for  $\alpha_D$  in a polymer coil. Thus, it is likely that  $\alpha_D$  is less than 0.60. It appears that the second virial coefficients,  $A_2$  and  $k_d$ , could also exhibit a stronger temperature dependence than usual since PETFE is not soluble in diisobutyl adipate at even relatively high temperatures. A further investigation



**Figure 12.** log-log plot of  $D_0^\circ$  vs.  $M_w$  for PETFE in diisobutyl adipate at 240 °C. Solid line denotes  $D_0^\circ = 3.35 \times 10^{-4} M_w^{-0.60}$ , with  $D_0^\circ$  and  $M_w$  expressed in  $\text{cm}^2/\text{s}$  and daltons, respectively.

on the temperature dependence of the solvent quality and its relationship with the polymer melt temperature, as well as eq 11 covering a broader molecular weight range, is under way.

In Figure 9, we have noted that in a plot of  $R_g$  vs.  $N_w$  the sizes on a per-weight basis for PE and PETFE appear to be comparable while the same sizes on a per-segment basis are not the same, with  $R_g(\text{per } -(\text{CF}_2\text{CF}_2\text{CH}_2\text{CH}_2)-\text{segment}) > R_g(\text{per } -(\text{CH}_2\text{CH}_2\text{CH}_2\text{CH}_2)-\text{segment})$ . As the molecular weight range covered for PETFE (□) is very small (by a factor of 2) when compared with other studies, e.g., PS (Δ, ○; by a factor of  $>100$ ), as shown in Figure 9, an  $\alpha_D$  value of  $\sim 0.6$  must necessarily be taken to be qualitative in nature. The precaution in no way detracts from our finding that PETFE is surprisingly flexible.

It should be noted that copolymers of tetrafluoroethylene (TFE) and ethylene (E) have been studied by means of high-temperature, high-resolution FT NMR [ $^1\text{H}$  (90 MHz) and  $^{19}\text{F}$  (84.68 MHz)],<sup>13</sup> infrared analysis,<sup>14</sup> and ESCA,<sup>15</sup> showing highly alternating structures with the equimolar copolymers alternating approximately 94% of the time. Thus, our analysis should remain valid for PETFE samples of comparable (equimolar) TFE/E compositions. Overall TFE/E composition variations can be taken into account by using experimentally measured refractive index increment.

Finally, in the cumulants method of data analysis, we obtained  $\mu_2/\bar{\Gamma}^2 \sim 0.1$ , suggesting a fairly narrow molecular weight distribution for our PETFE samples. The details are presented in paper 2.

#### IV. Conclusions

When the present PETFE samples are dissolved in diisobutyl adipate at 240 °C, polymer coils of fairly narrow molecular weight distribution are formed. The coil dimension appears to behave normally like those of other typical polymers such as polystyrene and poly(methyl methacrylate). Within the molecular weight range of our investigation, PETFE becomes an easy polymer to characterize since  $k_d \sim 0$  and  $\bar{D} = \Gamma/K^2$  over typical accessible scattering angles ( $\theta = 30-90^\circ$ ). Thus, with the relation  $D_0^\circ (\text{cm}^2/\text{s}) = 3.35 \times 10^{-4} M_w^{-0.60}$ , we can determine the molecular weight of PETFE using only one line-width measurement at a fixed scattering angle and at one finite concentration in the dilute solution regime by means of photon correlation spectroscopy. Furthermore, the cumulant method of data analysis is easily applicable for PETFE with such narrow molecular weight distributions. If we were interested only in the width of the MWD, the variance  $\mu_2/\bar{\Gamma}^2$  ( $\sim 0.1$ ) is a clear indicator of polymer molecular polydispersity.

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Registry No. (TFE)(E) (copolymer), 25038-71-5.

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## Light Scattering Characterization of an Alternating Copolymer of Ethylene and Tetrafluoroethylene. 2. Molecular Weight Distributions

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**ABSTRACT:** By combining static and dynamic properties ( $M_w$ ,  $A_2$ ,  $k_d$ ,  $R_g$ , and  $D_0^\circ$ ) of an alternating copolymer of ethylene and tetrafluoroethylene,  $-(CF_2CF_2CH_2CH_2)_x-$ , in diisobutyl adipate at 240 °C with a detailed analysis of the intensity-intensity time correlation function, we have been able to determine, for the first time, the molecular weight distribution (MWD) of an alternating copolymer of ethylene and tetrafluoroethylene (PETFE). A variety of Laplace inversion techniques, including multiexponential singular value decomposition (MSVD), a method of regularization (RILIE), and CONTIN, was used to obtain an estimate of the normalized characteristic line-width distribution function  $G(\Gamma)$ . The nonintrusive laser light scattering technique permits us to determine the molecular weight as well as the MWD of PETFE based on sound physical principles. Furthermore, in view of the simple  $\Gamma = DK^2$  (with  $\Gamma$ ,  $D$ , and  $K$  being the characteristic line width, the translational diffusion coefficient, and the magnitude of the momentum transfer vector, respectively) dependence and the second virial coefficient of diffusion,  $k_d \sim 0$ , the Laplace inversion used in the data analysis can be greatly simplified for determination of molecular weight and polydispersity of PETFE in diisobutyl adipate at 240 °C.

## I. Introduction

In the previous paper (1), we characterized the solution properties of an alternating copolymer of ethylene (E) and tetrafluoroethylene (TFE),  $-(CF_2CF_2CH_2CH_2)_x-$ , denoted PETFE, in diisobutyl adipate at 240 °C, using laser light scattering intensity and line-width measurements. From light scattering intensity measurements, we obtained  $\langle R_g^2 \rangle_z^{1/2} = 1.68 \times 10^{-1} M_w^{0.60}$ , with the  $z$ -average root-mean-square radius of gyration  $R_g$  [ $\equiv \langle R_g^2 \rangle_z^{1/2}$ ] and the weight-average molecular weight  $M_w$  expressed in units of Å and daltons, respectively. In combination with light scattering line-width measurements, we obtained  $D_0^\circ = 3.35 \times 10^{-4} M_w^{-0.60}$ , with the translational diffusion coefficient at infinite dilution expressed in units of  $\text{cm}^2 \text{s}^{-1}$ . In the present paper, the main steps are to obtain estimates

of the normalized characteristic line-width distribution function  $G(\Gamma)$  from the measured intensity-intensity time correlation function and to transform  $G(\Gamma)$  to the molecular weight distribution (MWD) by means of the experimentally determined scaling relation  $D_0^\circ = k_D M^{-0.60}$ . The main obstacle in the procedure is related to the relatively new method of data analysis: Laplace inversion of the electric field time correlation function:

$$g^{(1)}(K, \tau) = \int_0^\infty G(K, \Gamma) e^{-\Gamma(K)\tau} d\Gamma \quad (1)$$

Although Laplace inversion is a difficult ill-posed problem because of the bandwidth limitation of our instrument and the noise in  $g^{(1)}(K, \tau)$ , there exists a variety of approaches (in particular, the method of regularization) permitting us to obtain approximate forms of  $G(\Gamma)$  based on sound mathematical principles. Furthermore, several algorithms have undergone extensive tests using simulated data as well as actual experiments and have been applied to a variety of studies.<sup>1,2</sup> In an earlier laser light scattering study on the MWD of linear polyethylene,<sup>3</sup> we used the approach first developed by McWhirter and Pike,<sup>4,5</sup> while

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